



The Ceaseless Wind

*an introduction to the theory
of atmospheric motion*

John A. Dutton

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Mv. Nr. 112/2412

Dk 551.511
551.513
551.515

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AN INTRODUCTION
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